

# Types in CLEAN

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# Outline

- 1 Synonyms
- 2 Tuples
- 3 Records
- 4 Algebraic Types
- 5 Uniqueness typing
- 6 Arrays
- 7 Abstract data types
- 8 Classes

# Type aliases

```
:: Name ::= String
```

- Documentary nature  
→ improves readability
- Like typedef in C++

# Excercise – Synonyms

Write a new `icl` file, containing

- type synonyms `Length` for integer! Create a `Start` function to test it.

# Solution – Synonyms

```
:: Length ::= Int
```

# Tuples

```
:: Point2D ::= (Int, Int)
:: Point3D ::= (Int, Int, Int)
```

## Using tuples

```
mirror :: Point2D -> Point2D
mirror (x,y) = (y, -x)
```

# Tuples elements of different types

```
:: BagElement ::= (String, Int)
:: Bag ::= [BagElement]
```

```
insertBag :: Bag String -> Bag
insertBag [] string = [ (string, 1) ]
insertBag [(item,mult):xs] string
  | item == string = [(item, mult+1):xs]
  | otherwise      = [(item,mult):(insertBat xs string)]
```

## Excercise – Tuples

Write a new `icl` file, containing

- The previously declared Bag type.
- Write a function with the following signature:  
`multiplicity :: Bag String -> Int`  
returns the multiplicity of the given string or zero.
- A Start function to test it:

```
Start = multiplicity [("a", 1), ("b", 2)] "q"
```

## Solution – Tuples

```
multiplicity :: Bag String -> Int
multiplicity [] _ = 0
multiplicity [(item,mult):xs] string
  | item == string = mult
  | otherwise      = multiplicity xs string
```

# Example

## Declaration

```
:: Point = { x :: Int
            , y :: Int
            }
```

## Value

```
p1 :: Point
p1 = { x = 1
      , y = 1
      }
```

## Referencing

```
x1 :: Int
x1 = p1.x
```

# Comparison with tuple

## With record

```
:: Point = { x :: Int
             , y :: Int
             }
```

```
norm1 :: Point -> Int
```

```
norm1 point = point.x + point.y
```

## With tuple

```
:: Point ::= (Int, Int)
```

```
norm1 :: Point -> Int
```

```
norm1 (x,y) = x + y
```

# Records can be 'updated'

```
projectX :: Point -> Point
projectX point = { point & x = 0 }
```

- No need to refer to other fields' values
- Makes the usage of records flexible (fields can be added later without having to rewrite all functions)

## Exercise – Records

Define new records for pieces of different shapes:

- Square
- and Circle

Use type `Length`!

# Solution

```
:: Square = { side :: Length }  
:: Circle = { radius :: Length }
```

## Example – Direction

```
:: Direction = Left | Right
```

```
mirror :: Direction -> Direction
```

```
mirror Left = Right
```

```
mirror Right = Left
```

## Example – Point

```
:: Point = Point Int Int
```

```
Point :: Point -> Int
```

```
norm1 Point x y = x + y
```

### With tuple

```
:: Point := (Int, Int)
```

```
norm1 :: Point -> Int
```

```
norm1 (x,y) = x + y
```

# Example – Nat

```
:: Nat = Succ Nat | Zero
```

```
One = Succ Zero
```

```
Two = Succ One
```

```
pred :: Nat -> Nat
```

```
pred (Succ n) = n
```

```
double :: Nat -> Nat
```

```
//  $2 \star (1+n) = 1+1+(2 \star n)$ 
```

```
double (Succ n) = Succ (Succ (double n))
```

```
double Zero = 0
```

# Composite matching

```
:: Nat = Succ Nat | Zero

even :: Nat -> Bool
even Zero           = True
even (Succ Zero)    = False
even (Succ (Succ n)) = even n
```

## Example – BiNat

```
:: BiNat = One | Double BiNat |
   DoublePlusOne BiNat
six = Double ( DoublePlusOne One )

succ One           = Double One
succ (Double n)    = DoublePlusOne n
// 1 + (2n+1) = 2*(n+1)
succ (DoublePlusOne n) = Double (succ n)
```

# Parametric

```
:: Tree a = Node a (Tree a) (Tree a) | Leaf

height :: Tree a -> Nat
height Leaf      = 1
height Node l r = max (height l) (height r)
```

Notation:

- Type constructor: `Tree`
- Data constructor: `Node`

# Preorder traversal

```
:: Tree a = Node a (Tree a) (Tree a) | Leaf

preorder :: Tree a -> [a]
preorder Leaf      = []
preorder Node l r = [a] ++ (preorder l)
                    ++ (preorder r)
```

# Algebraic Types – Excercise

- Write an algebraic type `Color` which contains 4 different colours!
- Write a function that can calculate the number of the leaves in a given tree!
- Write a postorder traversal on the type `Tree` and save it a list.

# Algebraic Types – Solution

```
:: Color = Black | White | Red | Yellow
```

```
length :: Tree a -> Int
```

```
length Leaf      = 1
```

```
length Node l r = (length l) + (length r)
```

# Algebraic Types – Solution (cont)

```
preorder :: Tree a -> [a]
preorder Leaf      = []
preorder Node l r = (preorder l) ++
                    (preorder r) ++ [a]
```

# Benefits of unique types

- Normally destructive updates can't be done in Clean, because it violates referential transparency.
- Sometimes a destructive update is needed:
  - user interactions
  - writing files or on screen
  - etc.
- We can't refer to a uniqueness type twice, so we can safely update it.
- When a unique variable is updated, it is destroyed and a new one created.
- Memory can be reused.

# Input/Output

When we read a file it has a side-effect of changing the current position in the file. The next read from the file will return different value, so it violates referential transparency. If the read function returns a new file (with changed current position) we can make the original file unique.

```
writel2
  # f  = open("test.txt")
  # f2 = fwritec 'a' f
  = 1
```

# Arrays

- Contiguous blocks in memory
- Increases efficiency (constant time element selection)
- Increases risk of run-time errors

# Lazy vs. Strict Arrays

- Lazy: elements are evaluated only when directly referred at

```
:: LazyArray a ::= {a}
```

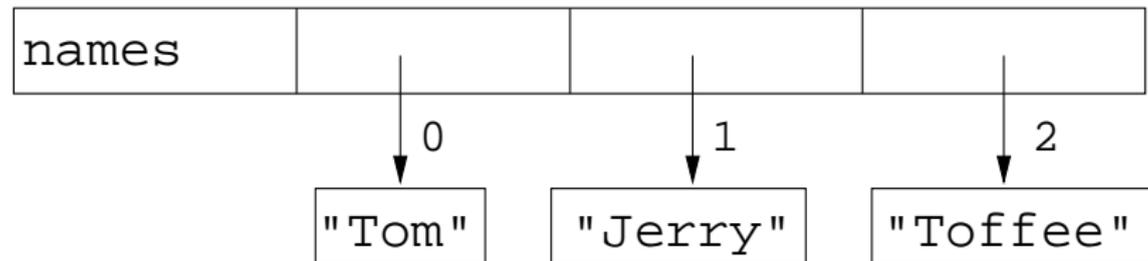
- Strict: elements are evaluated when the array is being referred at

```
:: StrictArray a ::= {!a}
```

# Boxed arrays

Only pointers to elements are stored in array itself

```
:: BoxedArray a ::= {a}
names :: BoxedArray
names = {"Tom", "Jerry", "Toffee"}
```



# Unboxed Arrays

Elements are stored directly in array itself

```
:: UnboxedArray a ::= {#a}
numbers :: UnboxedArray
numbers = {1, 2, 3, 5, 7, 11}
```

numbers	1	2	3	5	7	11
---------	---	---	---	---	---	----

# Array elements

Fields can be referred at directly by their indices  
(first index is 0):

```
thirdElement array = array.[2]
```

## Array comprehension

```
{ element \\ element <-: array }
```

Unique arrays can be updated:

```
uniqueArray :: *{Int} -> *{Int}
uniqueArray x = { x & [4] = 3, [3] = 4 }
```

## Excercise – Arrays

- Create an array `EmptyArray`, the size of 6 and contains only zeros!
- Write a function, `addAmount`, which takes an array, the amount of paint needed, and index, that indicates which colour's amount should be modified and updates the array respectively!

## Solution – Arrays

```
EmptyArray = { 0.0 \\ i <- [0..NumOfColors-1] }
```

```
addAmount array amount index  
# (value, array) = uselect array index  
= { array & [index] = value + amount }
```

```
// A bad solution. Two references to array  
addAmount array amount index  
= { array & [index] = amount + array.[index] }
```

# Declaration

The type's interface is placed in a separate definition module;  
user of the type sees only this module

```
stack.dcl
```

```
definition module stack
```

```
:: Stack a
```

```
Push  :: a (Stack a) -> Stack a
```

```
Pop   :: (Stack a) -> Stack a
```

```
top   :: (Stack a) -> a
```

```
Empty :: Stack a
```

# Implementation

Representation of type and implementation of functions is hidden from user of the module (hence the name abstract)

```
stack.icl
```

```
implementation module stack
```

```
:: Stack a ::= [a]
```

```
Push    e    s    = [ e : s ]
```

```
Pop     [ e : s ] = s
```

```
top     [ e : s ] = e
```

```
Empty           = []
```

# Usage

Representation and implementation can be changed without affecting the modules using this type

```
module stack_user

import stack

Start = top (Push 1 Empty)
```

# Abstract Types – Exercise

- Define and implement an abstract type `Queue` for queueing any types (a queue is a first in first out data-structure)! It has to have the following functions:
  - `EmptyQueue`
  - `insertItem`
  - `getFirstItem`
  - `removeFirstItem`
- Write a `Start` expression to test the new queue!

# Abstract Types – Solution

```
definition module queue
```

```
  :: Queue a
```

```
  EmptyQueue :: Queue a
```

```
  insertItem :: (Queue a) a -> (Queue a)
```

```
  getFirstItem :: (Queue a) -> a
```

```
  removeFirstItem :: (Queue a) -> (Queue a)
```

# Abstract Types – Solution

```
implementation module queue
```

```
import StdList
```

```
:: Queue a ::= [a]
```

```
EmptyQueue = []
```

```
insertItem queue item = queue ++ [item]
```

```
getFirstItem queue = hd queue
```

```
removeFirstItem queue = tl queue
```

# Abstract Types – Solution (cont)

```
import queue
```

```
Start = ( getFirstItem  
          ( insertItem  
            ( insertItem  
              ( insertItem EmptyQueue 8 )  
                2 )  
              3 )  
            )  
          )
```

'Ad hoc' polymorphism: we need the same set of functions for different types, but implementation depends on type

### pretty printing

```
class PrettyPrint a
where
  format :: a -> String
  concat :: a a -> String
  concat a1 a2 = (format a1) ++ ",
" ++ (format a2)
```

- We have to instantiate the class for all types we'd like to use it for
- Instantiation can differ from type to type

### Instantiation for Int

```
instance PrettyPrint Int
where
  format :: Int -> String
  format i = "Integer: " ++ toChar i
```

## Instantiation for Point

```
instance PrettyPrint Point
where
  format :: Point -> String
  format p = "Point: (x: " ++ (toChar p.x)
            ++ ", y: " ++ (toChar p.y)
            ++ ") "
```

- Member `concat` was derived from `format`
- Usage: user has to indicate that an instantiation of a particular class is needed

```
printList :: [a] -> String | PrettyPrint a
printList [ x : xs ] = (format x)
                    ++ printList xs
```

# Classes – Exercise

- Write a type class, `Measures a` that has to functions:
  - `circumference`
  - `surface!`
- Instantiate the class to both types of pieces!
- Add a field `price` to each type of pieces! Does it affect the functions you've just implemented?

# Classes – Solution

```
class Measures a
  where
    circumference :: a -> Real
    surface      :: a -> Real

instance Measures Square
  where
    circumference square = fromInt (square.side * 4)
    surface square       = fromInt (square.side * square.side)
```

## Classes – Solution (cont)

```
instance Measures Circle
where
  circumference circle
    = fromInt (2 * circle.radius) * 3.14
  surface circle
    = 3.14 * fromInt (circle.radius * circle.radius)

:: Square = { side :: Length
             , s_color :: Color, s_price :: Int
             }

:: Circle = { radius :: Length
            , c_color :: Color, c_price :: Int
            }
```